

Third Drag Prediction Workshop Results Using the NSU3D Unstructured Mesh Solver

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Results from the third AIAA drag prediction workshop on using the unstructured mesh Reynolds-averaged Navier–Stokes solver NSU3D are presented. Computations include a grid convergence study on a transonic wing–body and wing–body–fairing configuration at a fixed C_L condition using grids up to 41 million points, as well as an incidence sweep (drag polar) at fixed Mach and Reynolds numbers. A second set of results on a pair of closely related wing geometries is also described, including a grid convergence study at a fixed incidence and an incidence sweep (drag polar) for both wing geometries. For all cases, approximate second-order-accurate grid convergence characteristics are demonstrated, with overall accuracy and efficiency comparable with other structured, overset, and unstructured workshop calculations. However, it is found that differing grid-converged results may be inferred based on different families of self-similar coarse and fine-grid sequences, particularly for values such as absolute drag at a fixed incidence. More consistent grid convergence for idealized drag values (omitting induced drag) is observed, thus validating the procedure of performing grid convergence studies at a fixed C_L . These grid convergence issues are attributed to the large range of disparate scales that must be resolved in aerodynamic flows, and they point to the need for further advances in quantifying and resolving discretization errors for such problems.

I. Introduction

OVER the last five years, the AIAA Applied Aerodynamics Technical Committee has sponsored three drag prediction workshops (DPW), with the aim of assessing the current state-of-the-art computational fluid dynamics (CFD) solvers at predicting absolute and incremental drag changes on generic transonic transport aircraft configurations.

The first workshop, DPW 1, held in Anaheim, California in June 2001, employed the DLR-F4 wing–body geometry [1,2], due to its simplicity and relevance to modern transonic transport aircraft design studies, as well as due to the availability of publicly released experimental data. The second workshop, DPW 2, held in Orlando, Florida in June 2003, employed the slightly different DLR-F6 geometry, which included a wing–body configuration and a wing–body–nacelle–pylon configuration, both of which have been tested experimentally. DPW 2 thus offered the ability to study increments in drag between two similar configurations, as would typically be done in a design study. In both workshops, test cases were devised to mimic industrial design practices (these included fixed C_L single-point solutions, drag polars, and fixed C_L drag-rise data sets), and prediction of lift and moments were included, in addition to the general focus on drag prediction.

The results of the first workshop [1] revealed relatively large scatter between submitted participant calculations using a wide range of codes. The results of the second workshop [3] demonstrated substantially reduced scatter, particularly for drag-increment values between the two configurations, but still much higher levels than are generally desirable. Furthermore, with several notable exceptions, the bulk of the computational results in both workshops demonstrated relatively poor agreement with the experiment, especially in terms of lift versus incidence and moment prediction. Several

follow-up grid convergence studies with various structured and unstructured solvers [4–17] have also failed to resolve these discrepancies. These inconsistencies have been attributed, at least in part, to the existence of large pockets of separated flow on the DLR-F6 configuration. Although the configurations chosen for the two workshops consist of relatively simple geometries, the flow physics at the conditions of interest are more representative of off-design conditions, due to the regions of separated flow. In a typical design study, once such regions of separated flow are discovered, the geometry would be modified until these regions are removed or at least minimized, producing a cleaner cruise configuration. A principal objective of the third and most recent workshop, DPW 3, held in San Francisco, California in June 2006, was to test the hypothesis that the regions of separated flow were responsible for the wide scatter, poor grid convergence, and poor correlation with the experimental data of the various Reynolds-averaged Navier–Stokes (RANS) codes. Additionally, the workshop sought to establish the performance of RANS codes both on clean attached-flow cases and on more difficult off-design cases with substantial amounts of separated flow.

For DPW 3, a new wing–body fairing was designed [18] and added to the DLR-F6 wing–body configuration to suppress flow separation in the wing–body juncture region. The baseline DLR-F6 wing–body configuration was also retained as a test case, providing a bridge between the two most recent workshops and enabling the comparison of incremental values between clean and separated flow cases. Furthermore, to reduce the extent of the trailing-edge separation observed on the baseline DLR-F6 configuration studied in the DPW 2, the Reynolds number for these cases was raised from 3×10^6 to 5×10^6 in the DPW 3. Because no experimental data currently exist at this Reynolds number for these two configurations (with and without fairing), DPW 3 constituted a “blind” CFD test case, and emphasis was placed on examining grid convergence and scatter between the various participating entries.

A wind-tunnel test in the National Transonic Facility (NTF) at NASA Langley Research Center in Hampton, Virginia is planned for July 2007, which will be used to complement the numerical data sets obtained through DPW 3. The chosen Reynolds number of 5×10^6 for DPW 3 corresponds to the highest estimated Reynolds number achievable in the NTF for this model running in air (noncryogenically).

In addition to the two DLR-F6 wing–body configurations, a set of two wing-alone configurations were included as a second test case

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for DPW 3. The purpose of this second test case was, on one hand, to provide a simpler wing-alone geometry, which would enable the use of higher grid resolution, thus enabling a more complete resolution study, and to provide a well-behaved test case with no anticipated regions of separated flow. The use of two closely related wing geometries allowed for the assessment of predictions of increments in drag and other force and moment coefficients, as would typically be encountered in a design study.

The sequence of three workshops has enabled the assessment of the progress in state-of-the-art computational aerodynamics over the last half decade, made possible through advances in solver technology, grid-generation capabilities, and computing hardware. As an example, the size of the grids used has grown substantially with each new workshop, particularly for the unstructured-grid entries, with the largest unstructured grids in the DPW 1 containing under 10 million points and the largest unstructured grids in the DPW 3 exceeding 40 million points.

The purpose of this paper is to document the results obtained in the DPW 3 with the NSU3D unstructured mesh Reynolds-averaged Navier–Stokes solver. The NSU3D solver has been a participant in all three workshops [1,3,19] and has also been used in various follow-up studies, including comparison with other solvers [2,8,9], sensitivity studies, and extensive grid refinement studies.

II. Solver Description

The NSU3D code is an unstructured mesh multigrid RANS solver for high-Reynolds-number external aerodynamic applications. The NSU3D discretization employs a vertex-based approach, in which the unknown fluid and turbulence variables are stored at the vertices of the mesh and fluxes are computed on faces delimiting dual control volumes, with each dual face being associated with a mesh edge. This discretization operates on hybrid mixed-element meshes, generally employing prismatic elements in highly stretched boundary-layer regions and tetrahedral elements in isotropic regions of the mesh away from the aircraft surfaces. A single edge-based data structure is used to compute flux balances across all types of elements. The convective terms are discretized as central differences with added matrix dissipation. Second-order accuracy is achieved by formulating these dissipative terms as an undivided biharmonic operator, which is constructed in two passes of a nearest-neighbor Laplacian operator. In the matrix form, this dissipation is similar to that produced by a Riemann solver gradient-based reconstruction scheme and is obtained by replacing the difference in the reconstructed states on each side of the control volume interface by the undivided differences along mesh edges resulting from the biharmonic operator construction. These differences are then multiplied by the characteristic matrix to obtain the final dissipation terms.

The baseline NSU3D discretization employs a finite difference scheme to approximate the thin-layer form of the viscous terms for

the Navier–Stokes equations, although this is done in a multidimensional fashion, by computing a Laplacian of the velocity field [20]. The main approximation in this approach is the omission of the cross-derivative viscous terms and the assumption of a locally constant viscosity. The discretization of the full Navier–Stokes terms has also been implemented. This is achieved by first computing gradients of the flow variables at the grid vertices, using an edge-based loop, and then using a second edge loop to assemble the viscous flux balance at each vertex, based on these gradients. This approach results in an extended neighbor-of-neighbor stencil, which is less accurate than a nearest-neighbor stencil. However, a nearest-neighbor stencil discretization of second derivatives on mixed-element meshes requires the use of a cell data structure, whereas the current approach relies exclusively on the edge data structure. To improve the accuracy and stability of this discretization, a hybrid approach is adopted in which the second derivatives in the directions aligned with the incident mesh edges are computed using a nearest-neighbor stencil on the edges, whereas the remaining terms are computed using the extended stencil using the two-pass approach.

NSU3D incorporates the single-equation Spalart–Allmaras turbulence model [21], as well as a standard $k - \omega$ two-equation turbulence model [22]. All cases for DPW 3 were run using the Spalart–Allmaras turbulence model. Facilities for specified transition location based on the surface geometry are provided. Although this capability was employed in the DPW 2 [3,9], the cases for DPW 3 were all run fully turbulent.

The basic time-stepping scheme in NSU3D consists of a three-stage explicit multistage scheme. Convergence is accelerated by a local block-Jacobi preconditioner in regions of isotropic grid cells. In boundary-layer regions, in which the grid is highly stretched, a line preconditioner is employed to relieve the stiffness associated with the mesh anisotropy [23]. An agglomeration multigrid algorithm is used to further enhance convergence to steady state [20,24]. The Jacobi and line preconditioners are used to drive the various levels of the multigrid sequence, resulting in a rapidly converging solution technique. Figure 1a illustrates a typical convergence history for the DLR-F6 wing-body with fairing configuration at Mach = 0.75, incidence = 0.0 deg, and Reynolds = 5×10^6 , using the 5.6-, 14.6-, and 41-million-point grids supplied for DPW 3 and described subsequently. The solver is generally run for 500 multigrid cycles (up to 1000 cycles for more stringent cases with larger amounts of separated flow). The convergence is seen to be similar for all three grids, with only a slight decrease in the convergence rate as the grid resolution is increased. This is a property of the multigrid scheme, which is designed as an optimal solver to deliver convergence rates that are independent of the number of degrees of freedom.

On 16 AMD Opteron 242 processors, 500 multigrid cycles on the 5.0-million-point grid requires approximately 4.0 h of wall-clock time. On 128 CPUs of the NASA Columbia system (SGI Altix), this case requires 15 min of wall-clock time. The availability of the NASA Columbia supercomputer enables rapid turnaround for

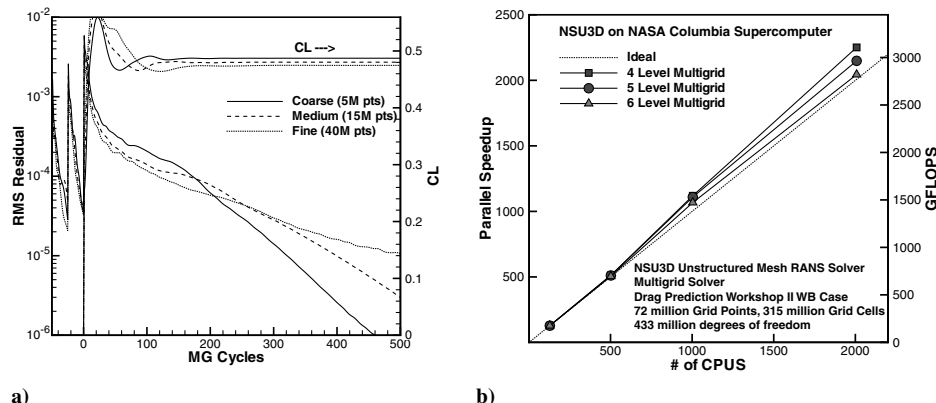


Fig. 1 Computational performance of NSU3D: a) multigrid convergence rate achieved on the wing-body-fairing configuration at Mach = 0.75, Reynolds = 5×10^6 , and $\alpha = 0.0$ deg for coarse, medium, and fine unstructured grids used in the DPW 3 workshop and b) scalability and computational rates achieved on the NASA Columbia supercomputer for NSU3D on a 72-million-point mesh for the wing-body test case, illustrating the effect of various multigrid levels on overall scalability.

Table 1 Computed lift and drag coefficients at Mach = 0.75, incidence = 0.0 deg, and Reynolds = 3×10^6 on various grids using the multidimensional thin-layer discretization and the extended-stencil full Navier–Stokes discretization for the wing–body configuration at Mach = 0.75, $\alpha = 0.0$ deg, and Reynolds = 3×10^6

| Grid size | Viscous terms | C_L | C_D | $C_{D_{\text{pressure}}}$ | $C_{D_{\text{friction}}}$ |
|----------------------|--------------------|--------|---------|---------------------------|---------------------------|
| One million points | Thin-layer approx. | 0.5055 | 0.02960 | 0.01661 | 0.01298 |
| One million points | Full Navier–Stokes | 0.4960 | 0.02921 | 0.01652 | 0.01269 |
| Three million points | Thin-layer approx. | 0.5012 | 0.02859 | 0.01568 | 0.01290 |
| Three million points | Full Navier–Stokes | 0.5020 | 0.02841 | 0.01571 | 0.01270 |
| Nine million points | Thin-layer approx. | 0.5141 | 0.02882 | 0.01592 | 0.01290 |
| Nine million points | Full Navier–Stokes | 0.5154 | 0.02867 | 0.01594 | 0.01273 |

solutions on very fine grids. For example, on 128 CPUs, a fine grid of 72 million points on the wing–body configuration requires approximately 4.5 h of CPU time to produce a converged solution. Figure 1b illustrates the scalability obtained on the NASA Columbia supercomputer for this 72-million-point grid, going from 128 to 2008 CPUs, demonstrating slightly superlinear speedup. A computational rate of approximately three Tflops was obtained on 2008 CPUs, using five multigrid levels. Using up to six multigrid levels modestly reduces the scalability and computational rates at high processor counts, due to the increased amount of communication required on the coarse-grid levels, but generally results in the fastest overall convergence. On 2008 CPUs, a solution on the 72-million-point grid could be obtained in 20 min of wall clock time (2 s per multigrid cycle).

III. Preliminary Sensitivity Studies

Before DPW 3, a sensitivity study of the NSU3D solver was carried out on the coarse, medium, and fine grids supplied for the DLR-F6 wing–body case of the DPW-2 workshop [17]. Relevant findings from this study are included herein, to justify the choices made in running NSU3D for DPW 3.

A. Thin Layer Versus Full Navier–Stokes Terms

The flowfield at the single condition of Mach = 0.75, incidence = 0.0 deg, and Reynolds = 3×10^6 (DPW-2 value) was computed on a family of progressively finer-resolution grids (1, 3, and 9 million points) using the original multidimensional thin-layer approximation in the baseline NSU3D code and also using the edge-based implementation of the full Navier–Stokes terms, as described previously. The computed values of the force coefficients are given in Table 1.

In all cases, the differences between the values computed with the thin-layer approximation and the full Navier–Stokes terms are minimal, corresponding to less than two counts of drag for the finer meshes of the sequence and small variations in the third significant figure of the lift coefficient. Note that for this case (DLR-F6 without fairing at a 3×10^6 Reynolds number), significant regions of flow separation are known to be present. However, based on the computed results for these cases, the multidimensional thin-layer assumption appears to be justified and little change in the solution is observed when going from the multidimensional thin layer to the full Navier–Stokes terms. All cases computed for DPW 3 described subsequently were run using the multidimensional thin-layer form of the viscous terms.

B. Distance-Function Sensitivity

The Spalart–Allmaras turbulence model requires knowledge of the distance to the nearest wall for each field grid point. The computation of this quantity has proved to be somewhat resource-intensive and prone to error. In fact, small differences are known to exist between the results generated by various approaches to solving this problem on the same grid. The resulting distance function is not necessarily smooth, because the location of the closest surface can change discontinuously as one proceeds outward in a concave region of the geometry, for example. This in turn implies that the accuracy of the computed distance may not scale with grid resolution in the same

manner as the overall discretization error and may contribute to anomalies in a grid convergence study. To this effect, we study the sensitivity of the solution to various approaches for computing the distance function, including an exhaustive search procedure, generally acknowledged to produce the most “exact” values, but perhaps involving nonsmooth variations in the distance function, and two partial-differential-equation-based methods. The first approach involves the solution of the eikonal equation [25], whereas the second approach involves the solution of a Poisson equation [26]. Although the first approach has been shown to produce distance-function values that are more closely related to those produced by the exhaustive search method, the results are known to be only first-order accurate in space. The Poisson equation approach, on the other hand, produces distance values that deviate substantially from the exhaustive search values at large distances away from the wall, but are close to these values in near-wall regions, and exhibit second-order discretization error. The Poisson equation approach is also the fastest distance-function-calculation method, because it can easily be parallelized and solved using the same multigrid approach used for the flow equations, whereas the eikonal equation is solved with a sweeping approach, which is difficult to parallelize, and is currently implemented as a preprocessing step running on a single processor. Both these approaches are more than an order of magnitude faster than the exhaustive search method and remain practical for very large mesh resolutions, in which the cost of the exhaustive search approach becomes prohibitive.

The lift and drag values computed on the same 1-, 3-, and 9-million-point grids discussed earlier, using the three different distance-function-evaluation methods, are given in Table 2 for the transonic flow conditions of Mach = 0.75, incidence = 0.0 deg, and Reynolds = 3×10^6 . In all cases, the values obtained using the eikonal-equation approach are almost indistinguishable from those obtained with the exhaustive search method. For example, there is always substantially less than a one-count difference in the computed drag between these methods. The computed lift values are consistent to three significant figures, with the smaller differences observed on finer grids. The Poisson equation approach produces more discrepancies in the computed force coefficients, showing variations of 2.8 counts of drag and approximately 1% difference in the computed lift coefficient on the coarsest mesh, although these differences are reduced on the finer grid. Overall, the eikonal-equation approach is the preferred method, because it differs very little from the exhaustive search approach, but is over an order of

Table 2 Computed lift and drag coefficients at Mach = 0.75 and incidence = 0.0 deg on various grids using three different approaches for computing the distance function

| Grid Size | Distance function | C_L | C_D |
|----------------------|-------------------|---------|---------|
| One million points | Exhaustive search | 0.50546 | 0.03139 |
| One million points | Eikonal equation | 0.50563 | 0.03138 |
| One million points | Poisson equation | 0.49915 | 0.03111 |
| Three million points | Exhaustive search | 0.50732 | 0.02942 |
| Three million points | Eikonal equation | 0.50751 | 0.02942 |
| Three million points | Poisson equation | 0.50452 | 0.02927 |
| Nine million points | Exhaustive search | 0.51410 | 0.02882 |
| Nine million points | Eikonal equation | 0.51404 | 0.02882 |

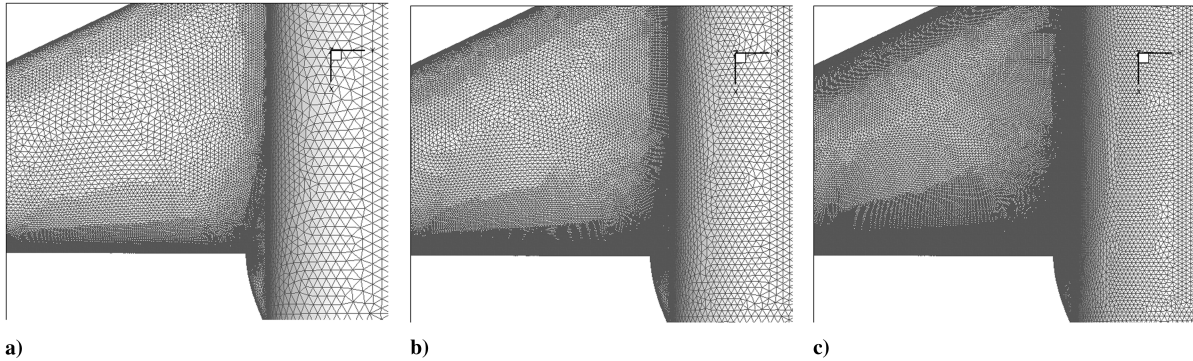


Fig. 2 Wing-body-fairing grid resolution near the wing-fuselage juncture for a) coarse mesh (5.6 million points total), b) medium mesh (14.6 million points total), and c) fine mesh (41 million points total).

magnitude faster in computing the distance function. On the other hand, this method is difficult to parallelize because it relies on a sweeping algorithm and is currently implemented as a sequential preprocessing step.

The eikonal-equation approach was used to calculate the distance function for all cases computed in the DPW 3 and described subsequently. On the finest grids considered, which contain slightly over 40 million points, the distance-function computation using the eikonal-equation approach required approximately 45 min on a single Itanium processor of the NASA Columbia machine (SGI Altix system).

IV. DPW 3: Case 1

A. Case-1 Description

The baseline DLR-F6 wing-body configuration was previously described in the context of DPW 2 [3]. This is a generic wing-body configuration representative of modern supercritical-wing transport aircraft design practices. The wing planform contains a trailing-edge break at the 41.1% span location, has a leading edge and quarter-chord sweep of 27.1 and 25 deg, respectively, and has an aspect ratio of 9.5. The original geometry has an acute angle of roughly 60 deg between the fuselage and the wing upper surface, which results in flow separation at the wing-body juncture. A new wing-body fairing was developed by Vassberg et al. [18] to suppress the side-of-body separation observed on the baseline wing-body geometry. The combination of the original wing-body geometry with and without the newly designed fairing constitutes the set of two geometries studied in case 1 for DPW 3. Case 1 consists of a grid convergence study on the DLR-F6 wing-body with and without fairing, at a fixed $C_L = 0.5$ condition, at $Mach = 0.75$, and at the higher Reynolds number of 5×10^6 (compared with 3×10^6 used in the DPW 2). A drag polar (on the medium grid) was also required by varying the incidence ($\alpha = -3.0, -2.0, -1.0, -0.5, 0.0, 0.15, 1.0$, and 1.5 deg), while holding the Mach and Reynolds number conditions fixed at the preceding values.

B. Grid Generation

A total of six different grids were used for case 1, consisting of a coarse, medium, and fine grid for each configuration. These grids were generated at NASA Langley Research Center using the VGRID grid-generation program [27] and made available on the DPW 3 web site under the designation “LaRC Unstructured Node-Based” [28]. The generated grids followed the gridding guidelines developed for the workshop, which are posted on the DPW web site [28] and summarized in [19]. These guidelines include a far-field boundary at 100 chord lengths away, a normal spacing at the wall of $y^+ < 1.0$ for the coarsest grids, with progressively smaller spacings on the finer grids, chordwise spacings at the wing leading and trailing edges of approximately 0.1% chord on the coarse mesh, and spanwise spacings of 0.1% at the wing root and tip on the coarsest mesh as well. A resolution of 8, 12, and 16 cells across the blunt trailing edge of the wing was specified for the coarse, medium, and fine grids,

respectively, and the overall size of the grids was targeted to grow by a factor of 3 when going from coarse to medium and from medium to fine. The medium grid was specified to be representative of the resolution level used in current industrial production runs.

An important consideration in a grid convergence study is to employ a sequence of grids using the same relative variations in spatial resolution and cell aspect ratios throughout the domain, with global refinement or coarsening between the various grids of this so-called family [29]. To achieve a self-similar family of grids, a set of spacings was specified in the VGRID grid-generation program using the source spacing method, and a global-grid-spacing rescaling was applied using the IFACT global spacing factor in VGRID [27] to obtain globally finer or coarser grids. Although this produces global variations in grid spacings, experimentation has shown that the desired changes in resolution are not always recovered exactly in all regions of the computational domain, although this is likely the best approximation to a self-similar family of grids that can be achieved using this methodology.[†]

Figure 2 illustrates the grid resolution in the critical wing-body juncture region for the wing-body-fairing geometry for the coarse, medium, and fine grids used in the NSU3D computations. The overall grid resolutions were substantially higher than those used in previous workshops, with the coarse grids containing approximately 5.6 million points, the medium grids containing 14.6 million points, and the fine grids exceeding 40 million points for both configurations. At this level, current industrial practice probably corresponds more closely to the coarse-grid resolution than to the medium-grid resolution. The precise specifications for these grids are given in Table 3. All these grids were transformed into hybrid prismatic-tetrahedral grids by merging triplets of tetrahedra in the boundary-layer regions into prismatic elements before the NSU3D computations.

C. NSU3D Results

In the absence of any experimental data, the numerical solutions were naturally concentrated on studying grid convergence. NSU3D was run on all three grids for each configuration at the fixed $C_L = 0.5$ condition. For the wing-body with fairing case, the complete incidence sweep was also run on all three grids. The convergence of NSU3D on all three grids at a fixed incidence of $\alpha = 0.0$ deg was previously discussed in Fig. 1, showing only minor dependence on the grid resolution. To compute the fixed C_L condition, a C_L driver is required, which periodically adjusts the incidence value to maintain the required lift value throughout the convergence process. Figure 3a compares the convergence obtained for a fixed α versus a fixed C_L case, in which the spikes in the residual plot correspond to step changes in α produced by the C_L driver. The constant lift case is initially run 200 multigrid cycles before engaging the C_L driver. At this point, a step change in the incidence is generated that produces a spike in the residual convergence history. Subsequent incidence adjustments occur at regular intervals, but become small enough that

[†]Private communication with E. M. Lee-Rausch, 2006.

Table 3 Description of grids used for the wing-body-fairing configuration

| | Wing-body-fairing | | | Wing-body | | |
|----------------------------------|-------------------|------------|-------------|------------|------------|-------------|
| | Coarse | Medium | Fine | Coarse | Medium | Fine |
| Global spacing ^a | 1.5 | 1.0 | 0.67 | 1.5 | 1.0 | 0.67 |
| Boundary points | 142,409 | 295,916 | 650,376 | 134,519 | 286,050 | 618,130 |
| Total grid points | 5,618,073 | 14,598,610 | 41,069,036 | 5,354,214 | 14,298,135 | 40,014,934 |
| Total tetrahedra | 33,037,458 | 85,850,911 | 241,486,342 | 31,481,575 | 84,078,830 | 235,263,704 |
| Tetrahedra (hybrid) ^b | 14,684,297 | 46,445,221 | 152,724,605 | 14,361,710 | 46,318,619 | 151,624,247 |
| Prisms (hybrid) ^b | 6,124,265 | 13,144,822 | 29,603,771 | 5,712,550 | 12,595,740 | 27,894,717 |
| Pyramids (hybrid) ^b | 38,738 | 57,007 | 98,737 | 34,940 | 53,443 | 88,448 |

^aGlobal spacing refers to the IFACT parameter, which controls the global spacing for VGRID.

^bHybrid cell numbers were obtained through postprocessing of VGRID output.

their effect on the convergence history is no longer perceptible, and the overall fixed C_L convergence rate is equivalent to the fixed incidence convergence rate.

In Fig. 3b, the computed surface-pressure distributions are shown at the break section (41.1% span) for the three progressively finer grids, showing minimal effect of grid resolution on these values. This degree of sensitivity is typical for most solvers on most configurations in the DPW 3 [19]. The computed surface skin-friction coefficients for the three different grid resolutions at the break section are shown in Fig. 3c, showing similarly low sensitivity of these values to the grid resolution. The addition of the side-body fairing for this case was successful in completely eliminating the side-of-body flow separation that was observed both numerically and experimentally on the geometry with no fairing [3,9,19]. The fully attached nature of the flow is depicted in the plot of Fig. 4a, which shows the streamlines in the region of the wing-fuselage-fairing juncture. However, a region of separated flow remains in the vicinity

of the trailing edge of the wing, as documented by the streamline traces in Fig. 4b and in the trailing-edge separation points logged in Table 4, which are determined by the location at which the skin-friction component in the direction normal to the trailing-edge span line vanishes. In Table 4, separation is seen to occur in the vicinity of 95 to 98% chord, with increased separation regions occurring on progressively finer meshes. Figures 5a–5c depict the lift versus incidence, drag polar, and pitching moment as functions of lift, computed on all three grids. Although the incidence sweep was only required on the medium grid, the use of all three grids permits the examination of the grid convergence effects over the complete incidence range. In general, the trends are well-behaved, with similar values and decreasing discrepancies when going to finer grids.

Figure 6a depicts the convergence history obtained on the medium grid for the wing-body case (without fairing) at a fixed incidence of $\alpha = 0.0$ deg. In this case, the residual does not fully converge, but rather exhibits a periodic behavior, which is attributed to the periodic

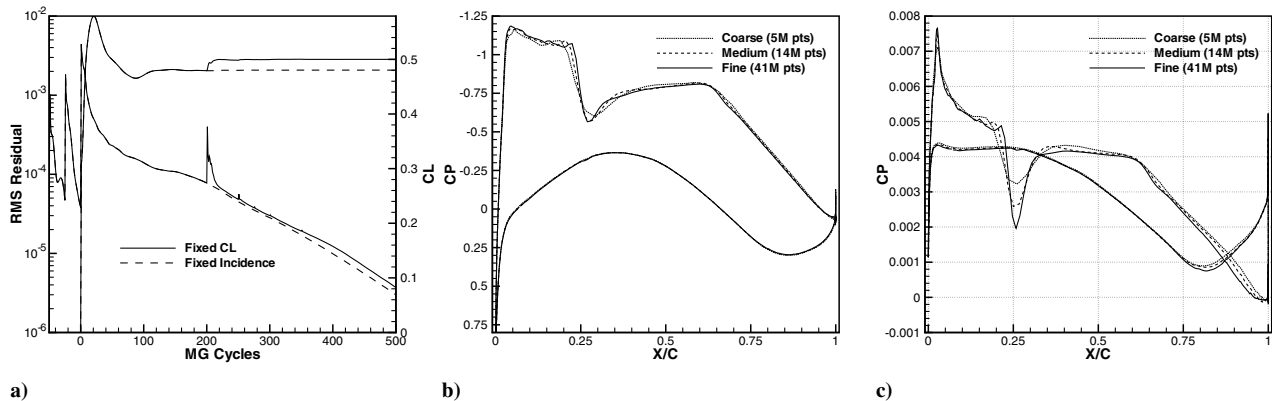


Fig. 3 Wing-body-fairing case: a) comparison of multigrid convergence for fixed-incidence and fixed-lift cases on the medium grid (14.6M points) for the wing-body-fairing geometry at Mach = 0.75 and Reynolds = 5×10^6 ; b) comparison of computed surface-pressure coefficients at 41.1% span location for coarse, medium, and fine grids for the wing-body-fairing geometry at Mach = 0.75, Reynolds = 5×10^6 , and $C_L = 0.5$; and c) comparison of computed skin-friction coefficients at the same location and conditions on coarse, medium, and fine wing-body-fairing grids.

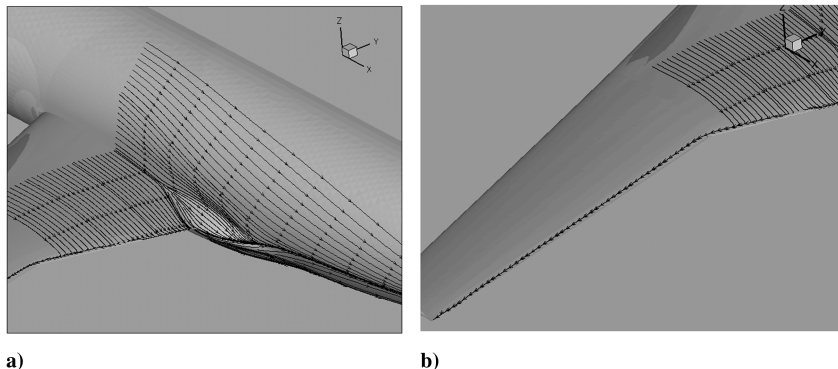


Fig. 4 Wing-body-fairing case: a) surface streamline traces on the coarse grid showing fully attached flow in the wing-body juncture region for the wing-body-fairing geometry at a fixed $C_L = 0.5$ condition and b) surface streamline traces on the coarse grid showing the trailing-edge separation region for the wing-body-fairing geometry at a fixed $C_L = 0.5$ condition.

Table 4 Location of trailing-edge separation as measured by the x/c chord location of vanishing skin friction in the direction normal to the trailing-edge span line for coarse, medium, and fine grids for the wing-body-fairing configuration at Mach = 0.75, Reynolds = 5×10^6 , and $C_L = 0.5$.

| Station | Span ($\eta = y/b$) | x/c coarse | x/c medium | x/c fine |
|---------|-----------------------|--------------|--------------|------------|
| 1 | 0.150 | 1.000 | 1.000 | 1.000 |
| 2 | 0.239 | 0.991 | 0.982 | 0.981 |
| 3 | 0.331 | 0.982 | 0.972 | 0.964 |
| 4 | 0.377 | 0.978 | 0.973 | 0.975 |
| 5 | 0.411 | 0.984 | 0.969 | 0.959 |
| 6 | 0.514 | 0.971 | 0.957 | 0.947 |
| 7 | 0.638 | 0.975 | 0.961 | 0.953 |
| 8 | 0.847 | 0.983 | 0.969 | 0.954 |

growing and shedding of the side-of-body separation region, as shown in the streamline traces of Fig. 6b. Figure 6c illustrates the extent of trailing-edge separation, which is qualitatively similar to that observed on the wing-body-fairing configuration. The precise computed separation locations are documented in Table 5 for this case on the coarse, medium, and fine grids. Convergence problems of this sort were experienced by various other entries in the DPW 3 for this geometry [19]. In spite of the lack of residual convergence, variations in the final force coefficients remain relatively small, as can be seen from Fig. 7a, in which the minimum and maximum values of the unsteady lift coefficient are plotted at each incidence. When plotted in drag-polar form, these differences are even smaller, as seen in Fig. 7b, whereas they are somewhat larger when the pitching moment is considered, as shown in Fig. 7c. Nevertheless, it was felt that the computed average force coefficients were accurate

enough to use in a grid convergence study and in examining increments between the wing-body-fairing and wing-body geometries.

Figures 8 and 9 compare the force and moment coefficients for the fixed $C_L = 0.5$ condition on the three grids for each geometry, as well as the incidence required to achieve this C_L condition. These values are plotted versus the inverse of the number of grid points to the $\frac{2}{3}$ power, with the understanding that for a family of self-similar coarse to fine grids, this quantity should be representative of the average cell size h to the second power. Thus, straight-line plots in these figures are indicative of second-order-accurate spatial convergence. The total drag convergence plots in Fig. 8a produce a relatively straight line for the wing-body-fairing geometry, with a somewhat less well-behaved plot for the wing-body configuration. When these plots are broken down into pressure and friction drag, a slight compensating effect is observed for the wing-body-fairing case, although the deviation from straight-line behavior is not too severe, as seen in Figs. 8b and 8c. On the other hand, the plots of the pitching-moment coefficient and incidence values in Figs. 9a and 9b result in relatively straight lines.

In [19], a figure of merit is defined for the various DPW 3 entries, which quantifies the deviation of these plots (broken down into pressure and friction drag) from straight-line behavior. The figure of merit computed for these NSU3D results is somewhat higher (i.e., worse) than eight other entries, but remains the lowest of all the unstructured-grid submissions. This is noteworthy, because the generation of a family of self-similar grids is much more speculative with unstructured-grid methodologies, in which the connectivity is not preserved and relative resolution variations may occur, compared with the generation of structured-grid families. Figures 10a–10c provide a comparison of the wing-body with and without fairing on

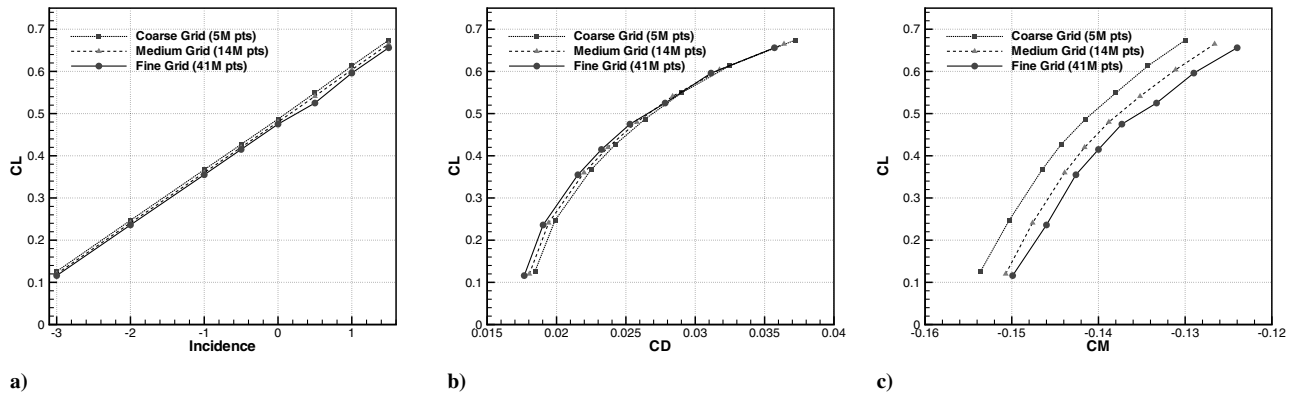


Fig. 5 Computed values of a) lift coefficient versus incidence, b) drag polar, and c) pitching-moment coefficient for the complete range of incidences for the wing-body-fairing geometry on coarse, medium, and fine grids.

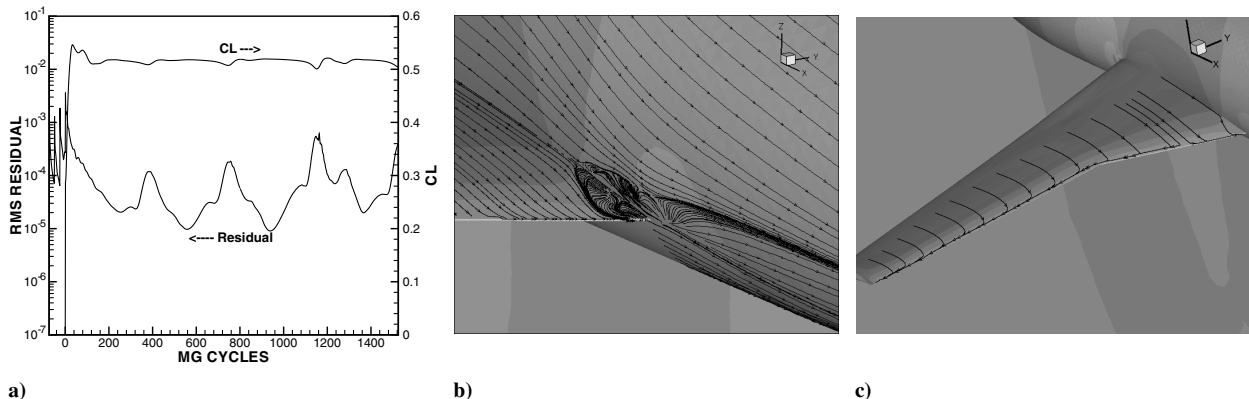


Fig. 6 Wing-body case: a) convergence rate on the medium grid for the wing-body configuration at Mach = 0.75, Reynolds = 5×10^6 , and $\alpha = 0.0$ deg, illustrating unsteady residual behavior; b) surface streamline traces on the coarse grid showing separated flow in the wing-body juncture region for the wing-body geometry at a fixed $C_L = 0.5$ condition; and c) surface streamline traces on the coarse grid showing the trailing-edge separation region for the wing-body geometry at a fixed $C_L = 0.5$ condition.

Table 5 Location of trailing-edge separation as measured by the x/c chord location of vanishing skin friction in the direction normal to the trailing-edge span line for coarse, medium, and fine grids for the wing-body configuration at Mach = 0.75, x/c , and $C_L = 0.5$

| Station | Span ($\eta = y/b$) | x/c coarse | x/c medium | x/c fine |
|---------|-----------------------|--------------|--------------|------------|
| 1 | 0.150 | 1.000 | 1.000 | 1.000 |
| 2 | 0.239 | 0.986 | 0.974 | 0.964 |
| 3 | 0.331 | 0.987 | 0.971 | 0.963 |
| 4 | 0.377 | 0.980 | 0.972 | 0.968 |
| 5 | 0.411 | 0.974 | 0.970 | 0.959 |
| 6 | 0.514 | 0.975 | 0.958 | 0.951 |
| 7 | 0.638 | 0.978 | 0.961 | 0.952 |
| 8 | 0.847 | 0.990 | 0.969 | 0.958 |

the medium grids, illustrating a consistent lift decrease at constant incidence, due to the addition of the fairing, and a decrease in the pitching moment. The differences in drag when plotted in drag-polar format are less substantial. Figure 9c depicts the computed drag increment between the two configurations at the constant $C_L = 0.5$ condition for the three grid resolutions, in which a value of two counts is reported on the medium and fine grids. By comparison, a total of 8 out of 13 workshop entries reported a drag increment between 0 and 5 counts at this condition, with five other entries reporting between 8 and 17 counts [19].

In summary, the case-1 results obtained using NSU3D indicate a reasonable level of grid convergence for both configurations, especially considering the difficulties associated with obtaining self-similar families of unstructured grids within a grid convergence

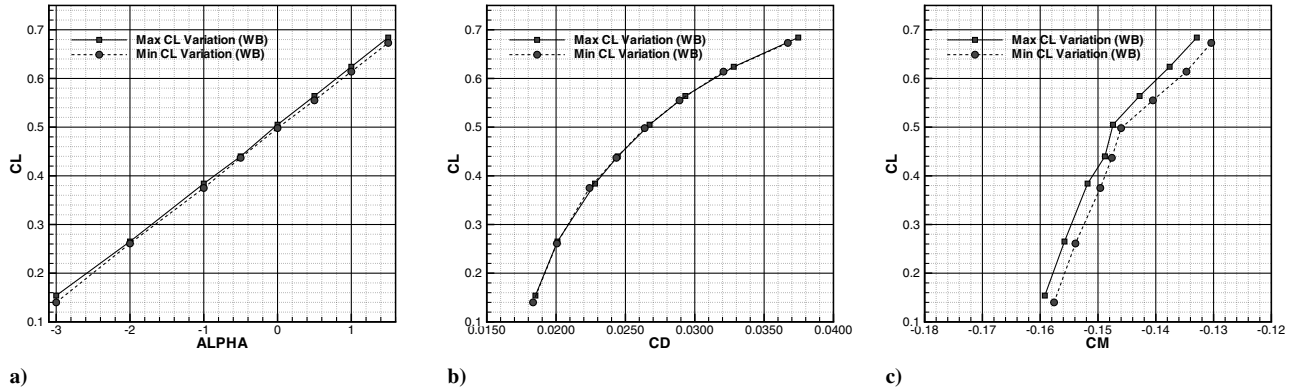


Fig. 7 Wing-body case: a) minimum and maximum values of the unsteady lift coefficient computed at various incidences; b) minimum and maximum values of the unsteady lift and drag coefficients, plotted in drag-polar format; and c) minimum and maximum values of the unsteady pitching moment versus the lift coefficient on the medium grid for the wing-body configuration at Mach = 0.75 and Reynolds = 5×10^6 .

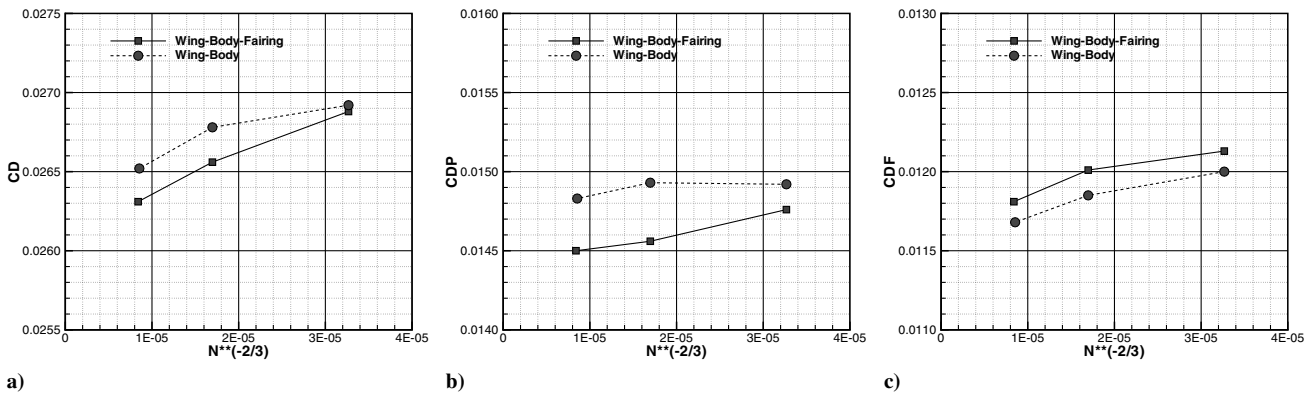


Fig. 8 Grid convergence plots for a) total drag, b) pressure drag, and c) friction drag for the wing-body-fairing and wing-body configurations at Mach = 0.75, Reynolds = 5×10^6 , and $C_L = 0.5$, plotted as functions of the number of grid points to the $-2/3$ power.

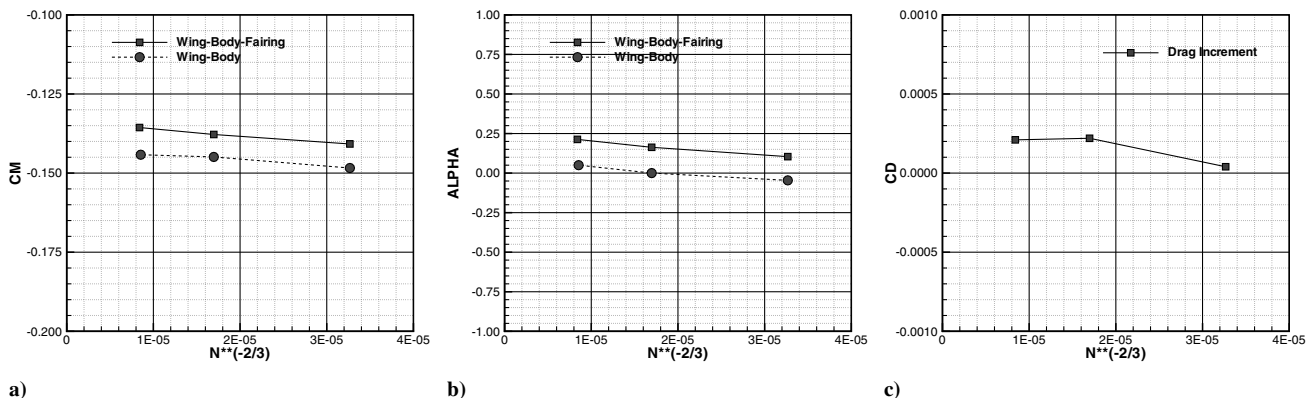


Fig. 9 Grid convergence plots for a) pitching moment, b) incidence, and c) drag increment for the wing-body-fairing and wing-body configurations at Mach = 0.75, Reynolds = 5×10^6 , and $C_L = 0.5$, plotted as functions of the number of grid points to the $-2/3$ power.

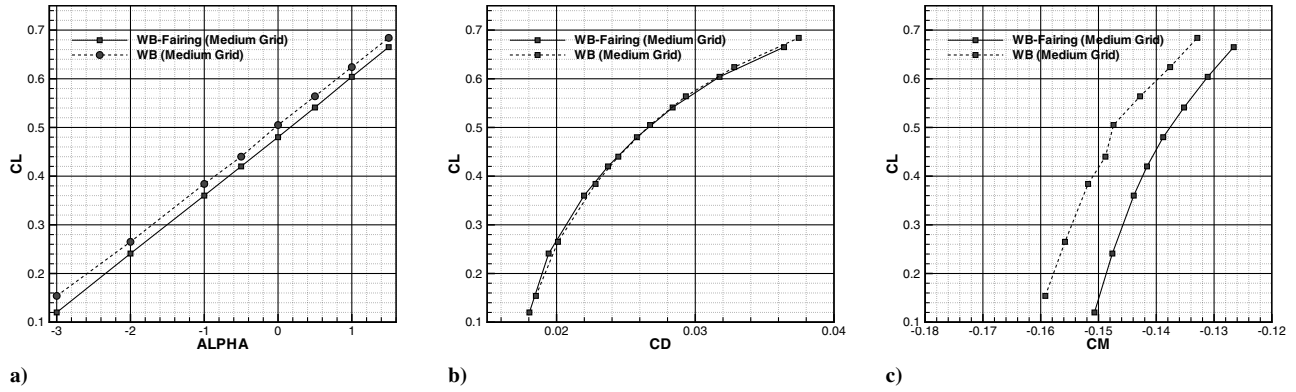


Fig. 10 Comparison of a) computed lift coefficient versus incidence, b) drag polars, and c) computed pitching-moment coefficients for the wing-body and wing-body-fairing cases on the medium grid (15 million points).

study. On the other hand, the wing-body configuration does not exhibit full and robust convergence, due to the side-of-body separation, as was noted by various other participants. This is partly in contrast with previous NSU3D results on this configuration from DPW 2 (at a Reynolds number of 3×10^6) and other grid refinement studies, in which convergence even in the presence of this side-of-body separation was not an issue [3,9,17]. Additionally, results on this configuration (albeit at the lower Reynolds number of 3×10^6) using a very fine grid of 65 million points, but generated using different local resolution settings (and notably with substantially increased spanwise trailing-edge resolution), have been found in previous work to result in substantially different predictions, with lift decreases of the order of 10% at the same incidence as the current and previous results on other fine grids using up to 72 million points [17]. Therefore, the effect of local variations in grid resolution can be expected to have a strong influence on predictions, particularly when substantial regions of separated flow are known to be present, and the measure of grid convergence based on a relatively limited family of coarse to fine grids may ultimately prove to be misleading.

V. DPW 3: Case 2

A. Case-2 Description

Case 2 is based on two generic wing-alone geometries designed by members of the DPW organizing committee. Both wings have a common trapezoidal planform shape, with no leading or trailing-edge breaks. The leading edge and quarter-chord sweep are 17.2 and 15 deg, respectively. The airfoil sections selected for the first wing geometry (wing 1) are representative of supercritical sections found on modern transport aircraft, whereas the second wing geometry (wing 2) represents a slight modification of wing 1 obtained through a single-point optimization process. A more detailed description of these geometries can be found in [19,28].

The test case consists of a grid convergence study at a fixed incidence of $\alpha = 0.5$ deg (as opposed to the fixed C_L condition of case 1) at a Mach number of 0.76 and a Reynolds number of 5×10^6 , in addition to a complete polar sweep for both geometries at incidences $\alpha = -1.0, 0.0, 0.5, 1.0, 1.5, 2.0, 2.5$, and 3.0 deg on the

medium grid. The relatively simple geometries of this test case enabled the use of a larger sequence of four rather than three coarse to fine grids, for a more complete grid convergence study. Additionally, the prediction of drag increments was targeted through the use of two closely related geometries.

B. Grid Generation

A total of eight different grids were used for case 2, consisting of a coarse, medium, fine, and extra-fine grid for each configuration. These grids were generated at NASA Langley Research Center using the VGRID grid-generation program [27] and made available on the DPW 3 web site under the designation “LaRC Unstructured Node-Based” [28]. The generated grids followed the same gridding guidelines developed for the workshop mentioned previously and are summarized in [19,28]. The same approach was used within the VGRID program for producing a family of self-similar coarse to fine meshes. The grid sizes range from 1.8 million points for the coarse mesh to 39 million points for the extra-fine mesh, with the principal grid characteristics detailed in Table 6 and illustrated in Fig. 11.

In addition to the cases run at the University of Wyoming, NSU3D was also used to compute case 2 at the Cessna Aircraft Company, using a different set of grids generated independently, but in the same fashion with VGRID. These grids, which are somewhat coarser than the NASA Langley Research Center’s VGRID submissions of Table 6, are described in Table 7. These grids are also available on the DPW web site [28] under the designation “Cessna Unstructured.” All these grids were transformed into hybrid prismatic-tetrahedral grids by merging triplets of tetrahedra in the boundary-layer regions into prismatic elements before the NSU3D computations.

C. NSU3D Results

The convergence of NSU3D on the four meshes of the wing-2 configuration described in Table 6 is depicted in Fig. 12a. The convergence degrades on the fine and extra-fine grids, but this is attributed to unsteadiness in the small regions of separated flow at the blunt trailing edge and has little effect on the overall force coefficient convergence. On all grids, the force coefficients are well-converged

Table 6 Description of grids used for wing 1 and wing 2 at the University of Wyoming

| | Wing 1 | | | | Wing 2 | | | |
|----------------------------------|------------|------------|------------|-------------|------------|------------|------------|-------------|
| | Coarse | Medium | Fine | Extra fine | Coarse | Medium | Fine | Extra fine |
| Global spacing ^a | 1.5 | 1.0 | 0.67 | 0.44 | 1.5 | 1.0 | 0.67 | 0.44 |
| Boundary points | 52,243 | 110,866 | 235,347 | 611,352 | 54,436 | 115,537 | 245,871 | 646,905 |
| Total grid points | 1,806,422 | 4,476,969 | 11,459,041 | 36,900,028 | 1,882,672 | 4,658,853 | 11,903,329 | 38,462,630 |
| Total tetrahedra | 10,639,646 | 26,368,110 | 67,463,143 | 217,160,940 | 11,088,290 | 27,437,220 | 70,081,360 | 226,386,508 |
| Tetrahedra (hybrid) ^b | 3,468,031 | 10,776,742 | 33,986,137 | 129,263,675 | 3,505,367 | 11,031,889 | 34,643,714 | 131,845,381 |
| Prisms (hybrid) ^b | 2,394,517 | 5,203,102 | 11,170,104 | 29,317,606 | 2,531,620 | 5,475,195 | 11,822,866 | 31,531,608 |
| Pyramids (hybrid) ^b | 24,247 | 36,401 | 67,307 | 112,201 | 22,864 | 39,178 | 60,294 | 105,474 |

^aGlobal spacing refers to the IFACT parameter, which controls the global spacing for VGRID.

^bHybrid cell numbers were obtained through postprocessing of VGRID output.

Table 7 Description of grids used for wing 1 and wing 2 at the Cessna Aircraft Company

| | Wing 1 | | | | Wing 2 | | | |
|----------------------------------|-----------|------------|------------|------------|-----------|------------|------------|------------|
| | Coarse | Medium | Fine | Extra fine | Coarse | Medium | Fine | Extra fine |
| Global spacing ^a | 1.5 | 1.0 | 0.67 | 0.5 | 1.5 | 1.0 | 0.67 | 0.5 |
| Boundary points | 35,270 | 70,449 | 139,768 | 236,291 | 33,993 | 67,138 | 134,164 | 227,109 |
| Total grid points | 983,633 | 2,417,082 | 6,138,245 | 12,748,678 | 947,409 | 2,325,884 | 5,963,713 | 12,419,567 |
| Total tetrahedra | 5,764,887 | 14,183,211 | 36,042,265 | 74,879,730 | 5,551,476 | 1,3647,064 | 35,016,693 | 72,945,687 |
| Tetrahedra (hybrid) ^b | 2,092,537 | 6,489,449 | 20,333,823 | 47,517,513 | 2,044,892 | 6,354,212 | 19,963,420 | 46,681,598 |
| Prisms (hybrid) ^b | 1,225,849 | 2,567,458 | 5,240,975 | 9,127,643 | 1,170,419 | 2,433,528 | 5,022,264 | 8,761,108 |
| Pyramids (hybrid) ^b | 10,249 | 16,909 | 28,601 | 41,131 | 9366 | 15,559 | 27,083 | 38,625 |

^aGlobal spacing refers to the IFACT parameter, which controls the global spacing for VGRID.

^bHybrid cell numbers were obtained through postprocessing of VGRID output.

(to four significant figures) within 500 multigrid cycles. Run times are similar to those described in case 1, ranging from 1 h on a cluster of 16 Opterons for the coarsest grid to 3 h using 96 CPUs on the NASA Columbia machine for the finest grid. The streamline traces for wing 2 in Fig. 12b show fully attached flow over the wing, with incipient separation at the trailing edge. Examination of the surface skin-friction values indicates fully attached flow, except on the extra-fine mesh, in which separation around 99.9% chord was observed.

The drag-polar calculation was computed using the fine grid for both configurations (15 million points), rather than the medium grid, as specified in the DPW 3 guidelines. Figure 13 illustrates the results of this exercise, comparing the values of lift, drag, and moment for both configurations throughout the range of incidences. The trends are generally consistent with those reported by other workshop participants. The wing-2 configuration, which is a single-point optimization of wing 1, produces slightly higher lift at $\alpha = 0.5$ deg (recall that the optimization was performed at constant lift), although these trends become reversed at higher incidences. The magnitude of

the pitching moment for wing 2 is also substantially reduced, compared with wing 1, over a broad range of incidences. Figures 14a and 14b depict the computed surface-pressure coefficients and skin-friction coefficients at the 55.1% span location for the various grids of the sequence for wing 1, with the only notable differences in going from coarse to fine grids in the resolution of the shock wave. Figure 14c illustrates the computed surface-pressure coefficients at the same span location on the fine grid (15 million points) for various incidences used in the drag-polar calculation. Note that the shock has moved forward and the wing is stalled at the highest incidence of 3.0 deg. Equivalent results are presented for wing 2 in Figs. 15a–15c, showing similar trends. The notable difference is the weakness of the shock for the optimized wing at $\alpha = 0.5$ deg, which is close to the single design point for wing 2 (which was optimized at constant C_L).

Figure 16 depicts the grid convergence results for both configurations on the four-grid sequence of Table 6, which were run at the University of Wyoming, and on the grid sequence of Table 7, which were run at the Cessna Aircraft Company. Concentrating initially on the first set of grids (Table 6), straight-line behavior

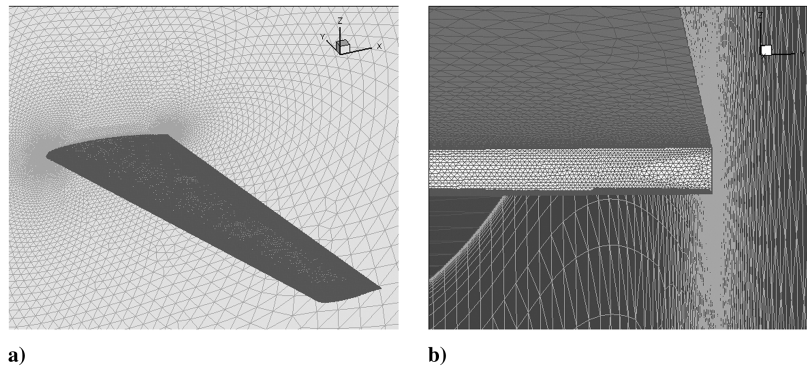


Fig. 11 Grid generation for wing-alone cases: a) fine grid on the wing-1 configuration, comprising a total of 15 million points and b) detail of the trailing-edge base resolution for the fine grid on the wing-1 configuration, containing approximately 16 cells across the blunt trailing-edge base.

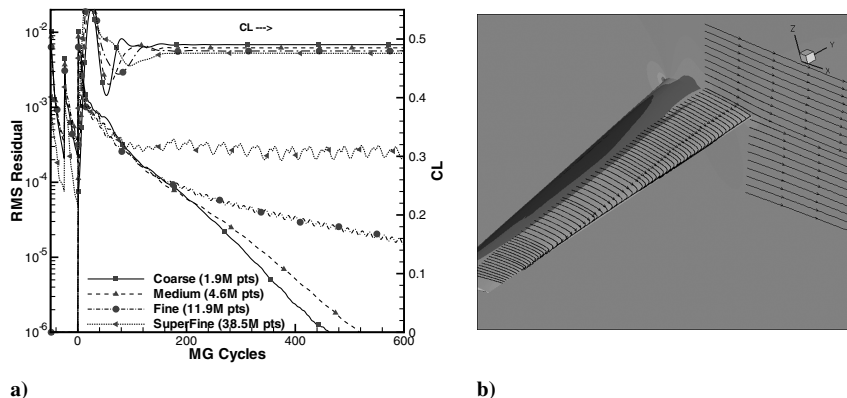


Fig. 12 Computation of the wing-2 case: a) multigrid convergence histories for the sequence of four grids for the wing-2 configuration and b) surface streamline traces for the wing-2 configuration on the coarse grid at Mach = 0.76, $\alpha = 0.5$ deg, and Reynolds = 5×10^6 .

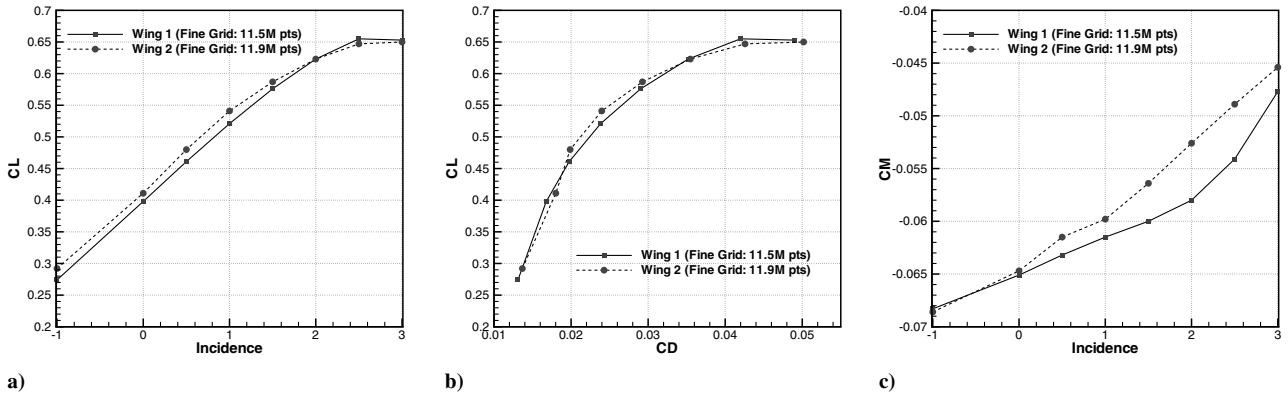


Fig. 13 Comparison of a) computed lift coefficient versus incidence, b) drag polars, and c) computed pitching-moment coefficients for wing 1 and wing 2 on the medium grid (15 million point).

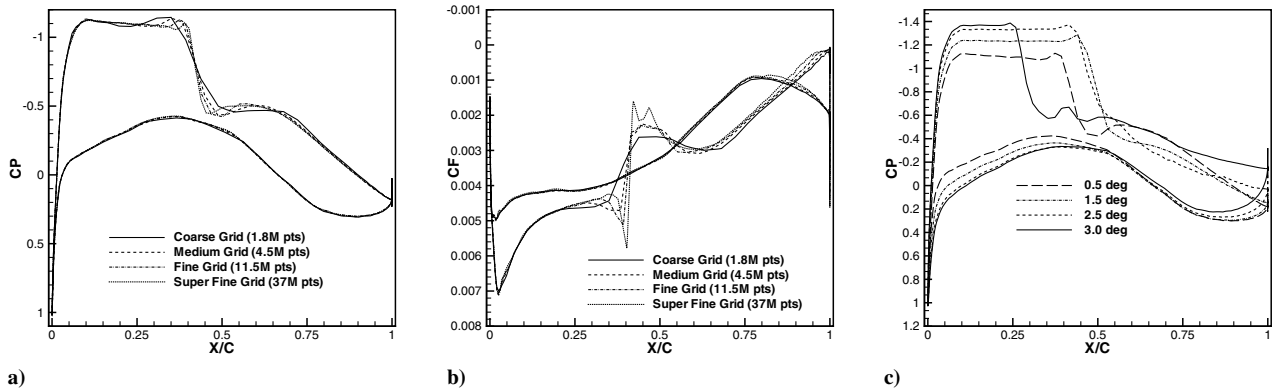


Fig. 14 Computed results for the wing-1 case: a) computed surface-pressure coefficients and b) skin-friction coefficients at the 55.1% span location at $Mach = 0.76$, $\alpha = 0.5$ deg, and $Re = 5 \times 10^6$ (on the four grids used in the grid refinement study for wing 1), and c) surface-pressure coefficients at the same location on the medium grid for wing 1 at various incidences, illustrating forward movement of shock at high incidences.

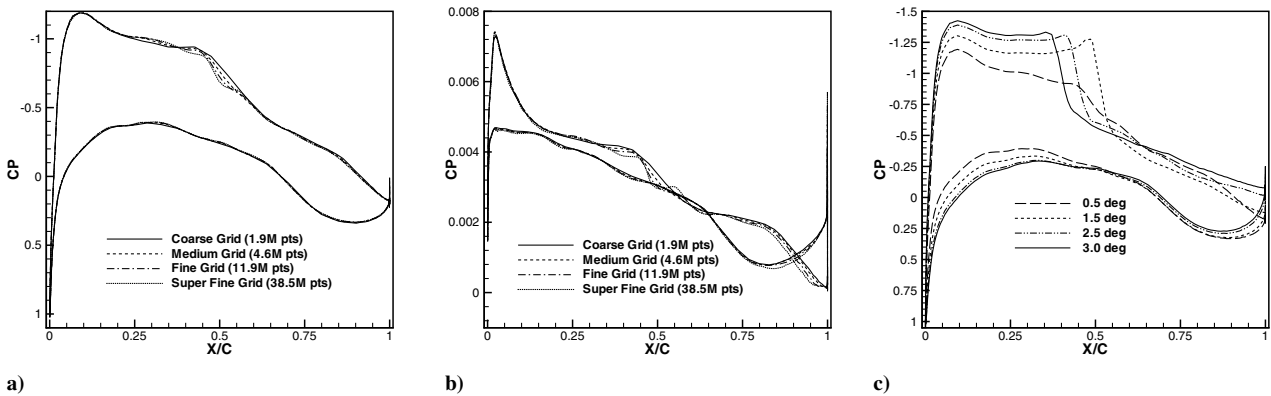


Fig. 15 Computed results for the wing-2 case: a) computed surface-pressure coefficients and b) skin-friction coefficients at the 55.1% span location at $Mach = 0.76$, $\alpha = 0.5$ deg, and $Re = 5 \times 10^6$ (on the four grids used in the grid refinement study for wing 2), and c) surface-pressure coefficients at the same location on the medium grid for wing 2 at various incidences, illustrating forward movement of shock at high incidences.

indicative of second-order-accurate spatial convergence is observed for virtually all quantities, including drag quantities broken down into pressure and friction values and the drag increment computed between the two configurations. The quality of this grid convergence is distinctly superior to that obtained for the wing-body configurations in case 1, and the addition of a fourth grid provides an even more convincing data set. In fact, these results displayed the most consistent second-order-accurate behavior out of all reported results for case 2 in the DPW 3, as determined by the figure-of-merit calculation performed in [19].

On the other hand, the results obtained using the second set of grids (cf. Table 7) are somewhat at odds with the former results. The plots corresponding to this latter set of grids does not collapse as neatly to a

straight-line behavior, although the overall deviation is still not too substantial (ranked third by the figure-of-merit method in [19]). This could possibly be attributed to a less than perfect self-similarity between the various grids of this family. Perhaps more concerning, however, is the fact that the two families of grids do not appear to be converging to the same continuum values in the limit of infinite mesh resolution. Some of these differences have been attributed to a reduced chordwise resolution of the second family of grids (cf. Table 7), which produces a less-well-resolved shock and generally higher lift and lower pitching-moment values, as seen in Figs. 17a and 17b. The drag increment computed on the two different grid families displays similar behavior, as seen in Fig. 18a. On the other hand, the idealized drag [defined as $C_{D_{ideal}} = C_D - C_L^2/(\pi AR)$,

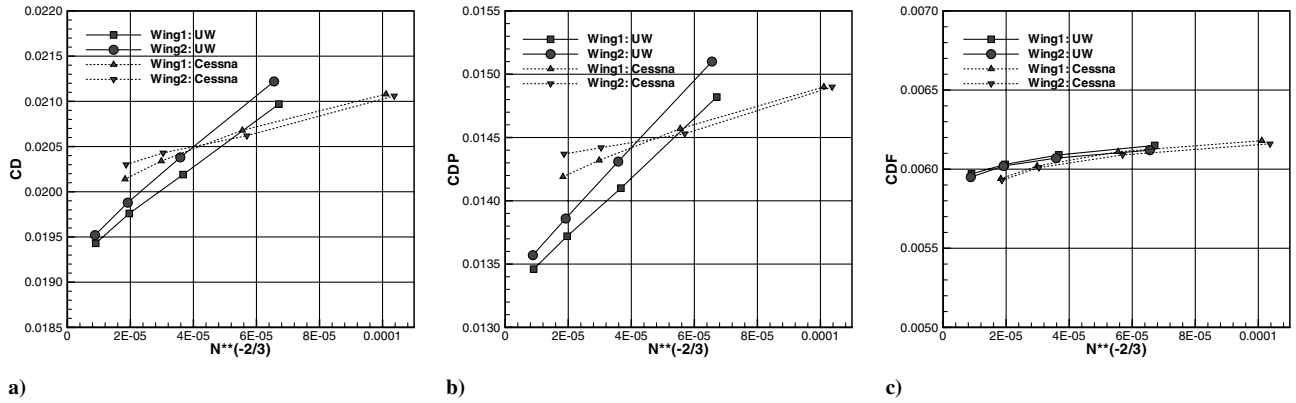


Fig. 16 Grid convergence plots for a) total drag, b) pressure drag, and c) friction drag for wing-1 and wing-2 configurations at Mach = 0.76, $\alpha = 0.5$ deg, and Reynolds = 5×10^6 , plotted as functions of the number of grid points to the $-\frac{2}{3}$ power for two families of grids.

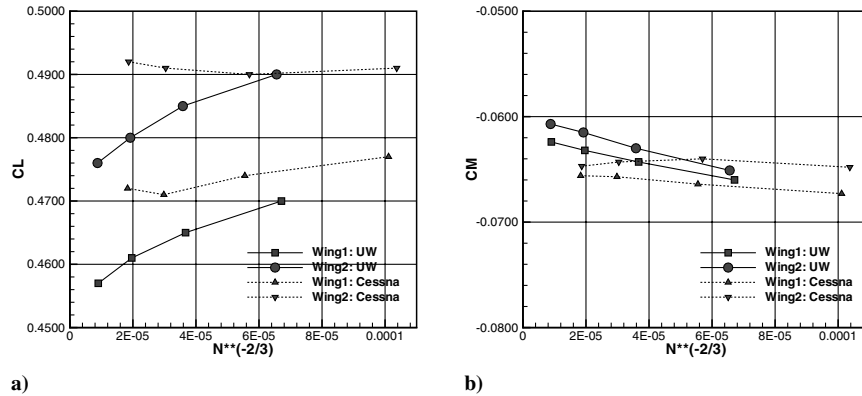


Fig. 17 Grid convergence plots for a) lift coefficient and b) pitching moment for wing-1 and wing-2 configurations at Mach = 0.76, Reynolds = 5×10^6 , and $\alpha = 0.5$ deg, plotted as functions of the number of grid points to the $-\frac{2}{3}$ power for two families of grids.

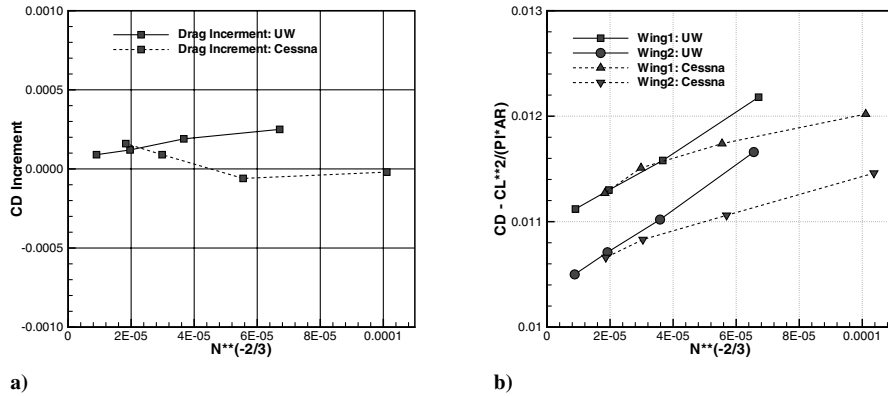


Fig. 18 Grid convergence plots for a) drag increment and b) idealized drag for wing-1 and wing-2 configurations at Mach = 0.76, Reynolds = 5×10^6 , and $\alpha = 0.5$ deg, plotted as functions of the number of grid points to the $-\frac{2}{3}$ power for two families of grids.

where AR denotes the planform aspect ratio] shows consistent drag convergence on both families of grids, as seen in Fig. 18b. This implies that the differences in drag prediction between the two families of grids are due to the induced drag associated with different lift predictions. Although this validates the approach taken in case 1 of performing the grid resolution study at constant C_L , mathematically, one should still expect grid convergence of all solution values (i.e., lift and drag) for sufficiently fine grids, and the current results once again illustrate the difficulty in ascertaining grid convergence across different families of grids, particularly for problems such as computational aerodynamics, in which the range of scales and thus grid resolution must necessarily vary by many orders of magnitude. This makes it unfeasible to fully resolve all regions through successive global mesh refinements without a good initial guess at the required local mesh resolutions, thus resulting in some

dependence on the initial mesh configuration or the definition of the family of meshes.

VI. Conclusions

Results from the third AIAA drag prediction workshop on using NSU3D have demonstrated solution accuracy and efficiency equivalent to other state-of-the-art structured, overset, and unstructured RANS solvers. Although changes in grid resolution have an almost trivial effect on computed surface distributions such as surface pressures and skin-friction coefficients, the overall effect on integrated quantities such as lift, drag, and pitching moment can be substantial, especially considering the accuracy requirement of aerodynamic design studies (i.e., drag to one-count accuracy). The NSU3D results from DPW 3 displayed consistent

second-order-accurate grid convergence compared with other DPW-3 entries, especially given the uncertainties inherent in generating families of self-similar unstructured grids. However, in case 2 of this workshop, as well as in previous grid refinement studies [17], different grid-converged results may be predicted using different families of grids. The range of scales inherent in computational aerodynamics problems, which may easily vary by over six orders of magnitude, make it unfeasible to fully resolve all regions of the computational domain through successive global refinements of an arbitrarily constructed initial grid, resulting in a dependence on the initial grid and resulting families of grids obtained by successive refinements. An obvious remedy may include the use of adaptive meshing, although the success of this approach rests on the ability to formulate adequate and robust refinement criteria. In this respect, adjoint-based error-estimation techniques offer some promise [30], although caveats remain, particularly considering the fact that these methods are based on a linearization of what may be an extremely nonlinear problem.

Finally, the third drag prediction workshop provides an objective assessment of the state-of-the-art computational aerodynamics. On one hand, our capabilities for generating and computing on ever-increasing grid sizes with faster turnaround times and producing more accurate solutions with less scatter are increasing continuously, whereas on the other hand, a complete understanding and quantification of the various sources of errors (including discretization, algebraic, and modeling errors) is still in its infancy.

Acknowledgments

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